the concentrations of triiodide and vanadic ions, and inversely proportional to the concentrations of the hydrogen and iodide ions. This result is in agreement with the postulation that the single rate determining step is one between hydrolyzed vanadic ions, $\mathrm{VOH}^{++}$, and iodine molecules.

Several possible rapid follow-up mechanisms have been suggested. The salt effect has been measured over the range of ionic strengths from 0.31 to 1.76 , and a possible explanation for its large negative magnitude has been advanced.
Los Angeles, Calif. Received April 23, 1936

# The Mechanism of Substitution Reactions. Substitution of Bromine and Chlorine in Phenylbromo and Phenylchloroacetic Acids by Chloride and Bromide Ions in Aqueous Solution 

By M. J. Young and A. R. Olson

When an optically active bromo compound is treated with chloride ion, a whole system of reactions is initiated. By making a kinetic study of the system of reactions which occurs when $l$ bromosuccinic acid is treated with chloride ion in aqueous solution, Olson and Long ${ }^{1}$ were able to prove the correctness of the theory of the mechanism of substitution reactions advanced by Olson, ${ }^{2}$ and by Bergmann, Polanyi and Szabo, ${ }^{3}$ according to which configurational inversion accompanies every single-step substitution.

The present study deals with the kinetics of the corresponding system of reactions produced by treating $l$-phenylbromoacetic acid with chloride ion in aqueous solution. The results provide additional confirmation of the above-mentioned theory.

The relations between the heats of activation of the various reactions in the succinic system, studied by Olson and Long, ${ }^{4}$ are again apparent in this system. The same is true of the temperature independent factors.

## Preparation of Materials

Phenylbromoacetic acid and phenylchloroacetic acid were prepared from mandelic acid (phenylhydroxyacetic acid) by treatment with the corresponding phosphorus pentahalides, following the procedure given by Walden and Bischoff. ${ }^{5}$ The acids were resolved by fractional crystallization of their morphine salts from methyl alcohol, following the procedure of McKenzie and Clough. ${ }^{6}$ The products were shown to be chemically pure by the usual analyses. Complete resolution was not obtained in all

[^0]cases but as is shown by the rate laws, optical purity is in no way essential. It is essential that the assumption that $l$-phenylchloroacetic acid and $l$-phenylbromoacetic acid have the same configuration be correct. This assumption is in accord with the opinion of those who have worked with such compounds.

## Apparatus

For all measurements of optical activity a laboratory constructed polarimeter of the Lippich type was used, with monochromatic light ( $\lambda$ 5461) obtained from a mercury arc and suitable filters. The angle of rotation was determined from the deflection of the image of an illuminated scale, four meters distant, produced in a small plane mirror mounted nearly on the axis of the analyser, and reflected into a telescope parallel to the optic axis by means of a periscope arrangement. This device enabled rotations to be read directly to $0.007^{\circ}(1 \mathrm{~mm}$. of scale) and estimated to $0.001^{\circ}$. A given setting can be duplicated to $0.005^{\circ}$. A thermostat provided with glass windows was mounted directly on the polarimeter so that tubes did not have to be removed tor observation.

## Experimental Procedure

Due to the slowness with which the phenylhalogenoacetic acids dissolve in water, the following procedure was adopted. A weighed amount of the active acid was dissolved in 0.4 cc . of methyl alcohol. To this solution was added the required amount of 2.00 N perchloric acid (about 10 cc .) followed, after re-solution had occurred, by the required amount of 2.00 N halogen acid (about 10 cc .). The addition of so small an amount of methvl alcohol has no observable effect on the reaction rates. All solutions were prepared at the temperature of the experiment. After the solution process, the material was transferred rapidly to a $30-\mathrm{cm}$. polarimeter tube and placed in the thermostat. Zero time was taken as the moment of addition of halide ion. The time interval between this addition and the first reading was never more than four minutes. In all experiments the concentrations are: active acid 0.015 M , halide ion 1.00 M , hydrogen ion 2.00 M , unless otherwise specified.
The Formation of Mandelic Acid from Phenylhalogenoacetic Acids.-The detailed mechanism


Fig. 1.-System of reactions occurring when $l$-phenylbromoacetic acid is treated with chloride ion in aqueous solution, assuming complete inversion accompanies each single-step substitution.
of the reactions between phenylbromoacetic acid or phenylchloroacetic acid and water, by which mandelic acid, hydrogen ion and halide ion are produced, is not completely understood in spite of the amount of investigation to which it has been subjected. $7,8,9$ The specific rate, measured by the rate of formation of hydrogen ion, is in accord with the assumption that the undissociated acid reacts more slowly than its ion. Measurement of the decrease of optical activity with time makes it necessary to suppose that the ion can react with water in either of two different ways, one reaction producing a $d$-mandelic acid, and the other an $l$-mandelic acid. The following mechanism can account for this effect and is at the same time in accord with the theory that inversion in configuration accompanies each single-step substitution.
(1)

$\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHOHCOOH}+\mathrm{H}^{+}+\mathrm{X}^{-}$(inversion at $\mathrm{C}(1)$ )
(2)
 $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHOHCOOH}+\mathrm{X}^{-}$(inversion at $\mathrm{C}(1)$ )
(3)

(4)


[^1](5)

(inversion at $\mathrm{C}(1)$ )
Reactions (1), (2) and the sequence (3), (4) lead to a mandelic acid of configuration opposite to that of the $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHXCOOH}$. The sequence (3), (5), involving a double inversion at $\mathrm{C}(1)$, leads to a mandelic acid of the same configuration as that of the $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHXCOOH}$. The relative amounts of levo and dextro mandelic acids depend on the relation between the specific rates of the various reactions under the conditions of the experiment.

Although we failed to isolate the postulated lactone, a similar compound is known to be formed in the hydrolysis of bromosuccinic acid.

When the hydrogen-ion concentration is large, this mechanism predicts that $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHXCOOH}$ will disappear at a specific rate $k_{1}+\left\{\left(k_{2}+k_{3}\right)\right.$ $\left.k_{\mathrm{a}} /\left(\mathrm{H}^{+}\right)\right\}$, where $k_{\mathrm{a}}$ is the dissociation constant of $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHXCOOH}$, and that $d$ and $l$ mandelic acids will appear at specific rates $k_{1}+\left\{\left(k_{2}+\right.\right.$ $\left.\left.k_{3} \beta\right) k_{\mathrm{a}} /\left(\mathrm{H}^{+}\right)\right\}$and $k_{3}(1-\beta) k_{\mathrm{a}} /\left(\mathrm{H}^{+}\right)$, respectively, where $\beta$ is the fraction of the lactone hydrolyzing by reaction (4) and ( $1-\beta$ ) the fraction hydrolyzing by reaction (5). If the specific rate of disappearance of $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHXCOOH}$ is represented by $K$, the specific rates of production of $l$ and $d$ mandelic acid can be represented by $K(\alpha)$, and $K(1-\alpha)$, respectively, where $\alpha=1-\left\{k_{3} \beta k_{\mathrm{a}} /\right.$ $\left.\left[k_{1}\left(\mathrm{H}^{+}\right)+k_{2} k_{\mathrm{a}}+k_{3} k_{\mathrm{a}}\right]\right\}$.

## Rate Laws

Following the system of reactions and the notation shown in Fig. 1, we can write the differen_
tial equations for the rate of change of the concentration of each substance.
(1) $\mathrm{d} x / \mathrm{d} t=-k_{1}\left(\mathrm{Br}^{-}\right) x+k_{1}\left(\mathrm{Br}^{-}\right) y+$

$$
k_{3}\left(\mathrm{Br}^{-}\right) z-k_{4}\left(\mathrm{Cl}^{-}\right) x-k_{5} x
$$

(2) $\mathrm{d} y / \mathrm{d} t=-k_{1}\left(\mathrm{Br}^{-}\right) y+k_{1}\left(\mathrm{Br}^{-}\right) x+$

$$
k_{8}\left(\mathrm{Br}^{-}\right) w-k_{4}\left(\mathrm{Cl}^{-}\right) y-k_{\mathrm{b}} y
$$

(3) $\mathrm{d} w / \mathrm{d} t=-k_{2}\left(\mathrm{Cl}^{-}\right) w+k_{2}\left(\mathrm{Cl}^{-}\right) z-$

$$
k_{3}\left(\mathrm{Br}^{-}\right) w+k_{4}\left(\mathrm{Cl}^{-}\right) y-k_{6} w
$$

(4) $\mathrm{d} z / \mathrm{d} t=-k_{2}\left(\mathrm{Cl}^{-}\right) z+k_{2}\left(\mathrm{Cl}^{-}\right) w-$

$$
k_{3}\left(\mathrm{Br}^{-}\right) z+k_{4}\left(\mathrm{Cl}^{-}\right) x-k_{6} z
$$

(5) $\mathrm{d} r / \mathrm{d} t=k_{5} \alpha x+k_{5}(1-\alpha) y+k_{f} \alpha w+k_{6}(1-\alpha) z$
(6) $\mathrm{d} s / \mathrm{d} t=k_{5} \alpha y+k_{6}(1-\alpha) x+k_{6} \alpha z+k_{6}(1-\alpha) w$
(7) $\mathrm{d}\left(\mathrm{Br}^{-}\right) / \mathrm{d} t=k_{4}\left(\mathrm{Cl}^{-}\right)(x+y)-$

$$
k_{3}\left(\mathrm{Br}^{-}\right)(w+z)+k_{5}(x+y)
$$

(8) d

$$
\begin{aligned}
& \mathrm{d}\left(\mathrm{Cl}^{-}\right) / \mathrm{d} t=-k_{4}\left(\mathrm{Cl}^{-}\right)(x+y)+ \\
& \quad k_{3}\left(\mathrm{Br}^{-}\right)(w+z)+k_{5}(w+z)
\end{aligned}
$$

For the determination of the angle of rotation only the quantities $(x-y),(w-z)$ and $(r-s)$ need be calculated, for $\theta=C_{1}(x-y)+C_{2}(w-$ $z)+C_{3}(r-s)$. For the evaluation of the six specific rates, a series of experiments was devised each involving only one unknown specific rate. This series, and the corresponding integrated rate laws, are shown in Table I.

## Table I

(1) Initial conditions: $(x-y)=(x-y)_{0},(w-z)=$ $0,(r-s)=0,\left(\mathrm{Cl}^{-}\right)=0,\left(\mathrm{Br}^{-}\right)=1 M,\left(\mathrm{H}^{+}\right)=$
$2 M$
Additional assumption: $k_{1} \gg k_{5}$ so that $k_{5}$ can be neglected. $\left(\mathrm{Br}^{-}\right)=$constant
Rate law: $\Theta / \Theta_{0}=e^{-2 k_{1}\left(\mathrm{Br}^{-}\right) t}$
(2) Initial conditions: $(x-y)=0,(w-z)=(w-z)_{0}$, $(r-s)=0,\left(\mathrm{Cl}^{-}\right)=0,\left(\mathrm{Br}^{-}\right)=0,\left(\mathrm{H}^{+}\right)=2 M$
Additional assumption: Since $\left(\mathrm{Cl}^{-}\right)$remains small, $k_{2}\left(\mathrm{Cl}^{-}\right)$can be neglected compared to $k_{B}$
Rate law: $\left(\theta-\theta_{\infty}\right) /\left(\Theta_{0}-\theta_{\infty}\right)=e^{-k_{6 t}}, \Theta_{\infty}=C_{3}$ $(w-z)_{0}(2 \alpha-1)$
(3) Initial conditions: $(x-y)=0,(w-z)=(w-z)_{0}$, $(r-s)=0,\left(\mathrm{Cl}^{-}\right)=1 M,\left(\mathrm{Br}^{-}\right)=0,\left(\mathrm{H}^{+}\right)=$ $2 M$
Additional assumption: $\left(\mathrm{Cl}^{-}\right)=$constant
Rate law: $\left(\Theta-\Theta_{\infty}\right) /\left(\Theta_{0}-\Theta_{\infty}\right)=e^{-\left[2 k_{2}\left(\mathrm{Cl}^{-}\right)+k_{6}\right] t}$, $\theta_{\infty}=C_{3}(w-z)_{0} k_{6}(2 \alpha-1) /\left\{2 k_{2}\left(\mathrm{Cl}^{-}\right)+k_{6}\right\}$
(4)

Initial conditions: $A=(x-y)=(x-y)_{0},(w-z)$ $=0,(r-s)=0,\left(\mathrm{Cl}^{-}\right)=0,\left(\mathrm{Br}^{-}\right)=0,\left(\mathrm{H}^{+}\right)=$ $2 M$
Additional assumptions: none
Rate law: $\left(\theta-\theta_{\infty}\right) /\left(A_{0}-\theta_{\infty}\right)=$ $e-\left(2_{k}, A+k_{b}\right) t+\left\{2 k_{1} A\left(1-e^{-k_{5} t}\right) / k_{b}\right\} \theta_{\infty}=C_{3}(x-y)_{0}$ $(2 \alpha-1) k_{5} /\left(2 k_{1} A+k_{5}\right)$
(i) Initial conditions: $(x-y)=0,(w-z)=(w-z)_{0}$, $(r-s)=0,\left(\mathrm{Cl}^{-}\right)=0,\left(\mathrm{Br}^{-}\right)=1 M,\left(\mathrm{H}^{+}\right)=$ $2 M$

Additional assumptions: (1) $k_{1} \gg k_{3}$ so that $\phi \mathrm{CHBr}-$ COOH is racemized as fast as it is formed; $i$. e., $(x-y)=0 ; k_{5}$ makes no contribution to $(r-s)$.
(2) $\left(\mathrm{Cl}^{-}\right)$is so small that $k_{2}\left(\mathrm{Cl}^{-}\right)$and $k_{4}\left(\mathrm{Cl}^{-}\right)$ are negligible.
(3) $\left(\mathrm{Br}^{-}\right)=$constant

Rate law: $\left(\theta-\Theta_{\infty}\right) /\left(\Theta_{0}-\theta_{\infty}\right)=e^{-\left[k_{s}\left(\mathrm{Br}^{-}\right)+k_{6}\right] t}, \theta_{\infty}$ $=k_{6}(w-z)_{0} C_{5}(2 \alpha-1) /\left(k_{5}\left(\mathrm{Br}^{-}\right)+k_{6}\right)$
(6) Initial conditions: $(x-y)=(x-y)_{0}=A,(w-z)$ $=0,(r-s)=0,\left(\mathrm{Cl}^{-}\right)=1 M,\left(\mathrm{Br}^{-}\right)=0$, $\left(\mathrm{H}^{+}\right)=2 \mathrm{M}$
Additional assumptions: (1) $k_{3}\left(\mathrm{Br}^{-}\right)$can be neglected,
(2) $k_{6} \ll k_{5}$,
(3) $\left(\mathrm{Cl}^{-}\right)=$constant,
(4) $\theta_{\infty}=0$ (experimentally true)

Rate law: $\theta / \theta_{0}=(1+R) e^{-Q(t)}-R e^{-\left[2 k_{2}\left(\mathrm{Cl}^{-}\right)+k_{5}\right] t}$ $R=\left\{C_{2} / C_{1}\right] k_{4}\left(\mathrm{Cl}^{-}\right) /\left[2 k_{1} A+k_{4}\left(\mathrm{Cl}^{-}\right)+k_{5}-\right.$ $\left.2 k_{2}\left(\mathrm{Cl}^{-}\right)-k_{6}\right]$
 $e^{\left.\left.-\left[k_{4}\left(\mathrm{Cl}^{-}\right)+k_{5}\right] t\right) /\left(k_{4}\left(\mathrm{Cl}^{-}\right)+k_{5}\right)\right] .}$
The rate laws for experiment series (1), (2), (3) and (5) follow in a perfectly straightforward manner from the differential equations; those for experiment series (4) and (6) involve an integral of the form

$$
I=\int_{0}^{t} e^{-(a+b) t+\left[a\left(1-e^{-b t}\right) / b\right] \mathrm{d} t}
$$

We have been unable to evaluate this integral exactly in terms of elementary functions. Olson and Long handled it by means of a series expansion and term by term integration. We have found the following procedure more convenient in this case. Integration by parts gives

$$
\begin{aligned}
I=\{ & \left(1-e-(a+b) t+\left[a\left(1-e^{-b t}\right) / b\right]\right\} /(a+b) \\
& +\left\{a \int_{0}^{t} e^{-(a+2 b) t+\left[a\left(1-e^{-b t}\right) / b\right] \mathrm{d} t}\right\} /(a+b)
\end{aligned}
$$

The second integral can be neglected for two reasons. The integrand is smaller by a factor $e^{b t}$, and the coefficient $a$ is small compared to 1 , in the time units employed. The error introduced by this neglect is never more than $0.3 \%$.

The constants appearing in expressions (1), (2), (3) and (5) can be evaluated by calculating one value from each observation and averaging the results in the usual manner, or by obtaining a value of the slope of the line

$$
\ln \left(\theta-\theta_{\infty}\right) /\left(\theta_{0}-\theta_{\infty}\right)=-k t
$$

using the method of least squares. The expressions (4) and (6) cannot be solved explicitly for the unknown specific rates $k_{5}$ and $k_{4}$, respectively. In these cases a value of the specific rate was determined by a trial and error process to fit one
observation; the remaining observations were plotted on a curve calculated using this constant, and agreement was found satisfactory in all cases. The results obtained are given in Tables IIVIII. The values of $k$ (calcd.) are those obtained from the activation energies and temperature independent factors shown in Table VIII. All times are in minutes unless otherwise specified.

| Results |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Table II |  |  |  |  |  |
| $k_{1}$ |  |  |  |  |  |
| $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHBrCOOH}+\mathrm{Br}^{-}=d-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHBrCOOH}+\mathrm{Br}^{-}$ |  |  |  |  |  |
| T, ${ }^{\circ} \mathrm{K}$. | No. of runs | $\underset{\substack{\left(\mathrm{Br}^{-}\right) \\ \text {moles } \\ \text { liter }}}{ }$ liter | $k_{1}$ | Mear eviatio | $k_{1}$ calcod. |
| 288.1 | 2 | 0.984 | 0.004358 | 0.5 | 0.004363 |
| 298.1 | 2 | . 208 | . 01198 | . 1 |  |
| 298.1 | 3 | . 965 | . 01268 | . 3 | . 01251 |
| 303.23 | 2 | . 965 | . 01984 | . 3 | . 0209 |
| 307.02 | 2 | . 964 | . 02974 | 1 | . 03020 |
| 310.70 | 1 | . 960 | . 04294 |  | . 04294 |
| Table III |  |  |  |  |  |
| $k_{6}$ |  |  |  |  |  |
| $\xrightarrow{l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHClCOOH}+\mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{Cl}^{-}} \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHOHCOOH}+$ |  |  |  |  |  |
| T. ${ }^{\circ} \mathrm{K}$. |  | $\begin{aligned} & \text { No. of } \\ & \text { runs } \end{aligned}$ | ${ }^{\text {k }}$ |  | $\begin{gathered} \text { Mean } \\ \text { deviation. } \% \end{gathered}$ |
| 323.1 |  | 2 | $2.20 \times 10$ |  | 2 |
| 308.1 |  | 2 | $3.65 \times 10$ |  | 2 |
| 298.1 |  | 2 | $1.03 \times 10$ |  | 2 |

## Table IV

|  |  |  | $k_{2}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $l-\mathrm{C}_{6}$ | , | $\mathrm{COOH}+\mathrm{Cl}$ |  | ${ }_{8} \mathrm{H}_{5} \mathrm{CHClCOO}$ | $\mathrm{H}+\mathrm{Cl}^{-}$ |
|  |  | $K_{\text {obed. }}=$ |  |  | Mean deviation, |
|  |  | $2 k_{2}\left(\mathrm{Cl}^{-}\right)+k_{6}$ | (c) | ${ }^{2}$ |  |
| 308.1 | 2 | $5.067 \times 10^{-4}$ | 2.00 | $1.178 \times 10^{-4}$ | 1.6 |
| 323.1 | 2 | $2.660 \times 10^{-3}$ | 2.00 | $6.100 \times 10^{-4}$ | 1.5 |




Table VIII

| Reaction | $E_{\text {eal. } / \text { mole }}$ | $A \times 10^{-9}$ (sec. - <br> moles-' liters) |
| :--- | :--- | :---: |

No values of $E$ and $A$ for the hydrolysis reactions (Tables III and VI) were calculated for they would be of doubtful significance since the specific rates are complex averages over several reactions. The listed probable errors are mean deviations from the average of the values of $E$ calculated for each temperature interval.

It can be shown that the introduction of the assumption of incomplete inversion in configuration, giving rise to the system of reactions appearing in Fig. 2, where the Greek letters represent in each case the fraction of the reaction occurring without inversion, results in an alteration of the rate laws which is not detectable except in the case of expression 6. In this case the new rate law is

$$
\begin{gathered}
\Theta / \Theta_{0}=(1+R) e-Q(t)-R e-\left[2 k_{8}\left(\mathrm{Cl}^{-}\right)+k_{t}\right] t \\
\text { where } R=C_{2} k_{4}\left(\mathrm{Cl}^{-}\right)(1-2 \epsilon) / C_{1}\left[2 k_{1} A+\right. \\
\left.k_{4}\left(\mathrm{C}^{-}\right)(1-2 \epsilon)+k_{5}-2 k_{2}\left(\mathrm{Cl}^{-}\right)-k_{8}\right] \\
Q(t)=\left[2 k_{1} A+k_{4}\left(\mathrm{Cl}^{-}\right)(1-2 \epsilon)+k_{5}\right] t- \\
\left\{2 k _ { 1 } A \left(1-e^{\left.\left.-\left[k_{4}\left(\mathrm{Cl}^{-}\right)+k_{\mathrm{i}}\right] t\right) /\left[k_{4}\left(\mathrm{Cl}^{-}\right)+k_{5}\right]\right\}}\right.\right.
\end{gathered}
$$

The effect which this modification has on the calculated value of $\theta$ for various times and for various values of $\epsilon$ is shown in Table IX for the

| Table IX |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Time } \\ & \text { min. } \end{aligned}$ | $\underset{\epsilon}{\theta} \mathrm{cm}$ |  | $e=0.0 \overline{0}$ | $t \stackrel{\Delta \Theta}{=} 0.07$ |
| 0 | $-15.76$ | 0 | 0 | 0 |
| 10 | 11.18 | 0 | +0.01 | +0.01 |
| 20 | 7.27 | +0.01 | $+.02$ | +. 03 |
| 30 | 3.98 | - . 02 | $-.03$ | . 00 |
| 40 | 1.21 | $-.03$ | -. 04 | -. 05 |
| 50 | $+1.09$ | . 03 | -. 06 | -. 07 |
| 60 | 2.45 | $-.03$ | -. 06 | -. . 08 |
| 70 | 4.52 | -. . 03 | -. 05 | $-.09$ |
| 80 | 5.75 | -. . 03 | -. . 05 | -. 08 |
| 90 | 6.75 | -. 03 | $-.04$ | -. .08 |
| 100 | 7.54 | -. 02 | $-.03$ | -. 07 |
| 150 | 9.48 | -. 01 | -. 02 | -. 03 |
| 200 | 9.72 | -. .01 | -. 01 | -. . 01 |



Fig. 2.-System of reactions occurring when $l$-phenylbromoacetic acid is treated with chloride ion in aqueous solution, assuming some substitution without inversion can occur.
experiments at $322.54^{\circ} \mathrm{K}$. The curve calculated for $\epsilon=0$ on which the experimental points have been superimposed is shown in Fig. 3. ( $\Delta \theta$ is taken positive when the value for $\epsilon=0$ is larger in absolute magnitude than that for $\epsilon \neq 0$.)

Since the average deviation of the experimental points from the calculated curve is 0.06 cm . with no trend, one can conclude that inversion is complete within the limits of detectability ( $5 \%$ ). The rather large limits on $\epsilon$ are a result of the small value of $A$, the initial concentration of bromo acid, made necessary by its slow solubility. $\Delta \theta$ is directly proportional to $A$.

## Discussion of Results

The results obtained are compared with those of Olson and Long ${ }^{4}$ in Table X.

Table X

| Reaction | Activation energy cal./mole |  |  | Collision number $\times 10^{-9}$ sec. ${ }^{-1}$ moles ${ }^{-1}$ liters |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Phenylacetic system | Succinic system | $\triangle$ | Phenylsystem system | Succinic | tio |
| $1 \mathrm{BrA}+\mathrm{Br}^{-}$ | 17,971 | 21,800 | 3829 | 3.13 | 14. | 4.76 |
| $2 \mathrm{ClA}+\mathrm{Cl}^{-}$ | 21,683 | 24,770 | 3087 | 4.74 | 8.42 | 1.78 |
| $3 \mathrm{ClA}+\mathrm{Br}^{-}$ | 20,016 | 23,540 | 3524 | 1.90 | 6.24 | 3.28 |
| $4 \mathrm{BrA}+\mathrm{Cl}$ | 19,805 | 23,650 | 3845 | 6.93 | 39.5 |  |

(1) The difference between the activation energies of the two series is nearly the same for all reactions, although it is somewhat larger for the bromo acids than for the chloro acids. This 3600 calories is a composite of the alterations in bond strength and resistance to inversion brought about by substituting $-\mathrm{CH}_{2} \mathrm{COOH}$ for $\mathrm{C}_{6} \mathrm{H}_{5}$ in the reacting molecule. Nothing quantitative can be said about the relative contributions of the two factors.
(2) The fact that the activation energy of the exchange reactions (the same for both within experimental error) is closer to that of $\mathrm{ClA}+\mathrm{Cl}^{-}$ than to that of $\mathrm{BrA}+\mathrm{Br}^{-}$may mean that the unstable intermediate $(\mathrm{BrACl})^{-}$, where A is the rest of the molecule resembles ( ClACl$)^{-}$more closely than $(\mathrm{BrABr})$ -


Fig. 3.-Angle of rotation plotted against time for the reaction between $l$-phenylbromoacetic acid and chloride ion in aqueous solution at $322.54^{\circ} \mathrm{K}$.
(3) The collision numbers of reactions involving $\mathrm{Cl}^{-}$are larger than those involving $\mathrm{Br}^{-}$, while those involving bromo acids are larger than those involving chloro acids, and the collision number of the exchange reaction $\mathrm{BrA}+\mathrm{Cl}^{-}$is larger than that of $\mathrm{ClA}+\mathrm{Br}^{-}$in the ratio one would expect from the two tendencies in combination.

A calculation of the total number of collisions for comparison with the observed collision number
is somewhat arbitrary because of the uncertainty in collision diameter. The arbitrary selection of a value 1.75 times the length of the bond to be formed, leads to a steric factor of from $1 / 40$ to $1 / 10$. The face centered addition of $\mathrm{X}^{-}$at $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHY}$ COOH leads to an orientation factor of less than $1 / 2$ for $\mathrm{C}_{0} \mathrm{H}_{5} \mathrm{CHYCOOH}$; solvation of $\mathrm{X}^{-}$ may introduce an additional orientation factor. Furthermore, one must take into account the efficiency of transfer between translational and vibrational energy which Rice ${ }^{10}$ has found to vary widely from case to case. The most that one can say is, that there is nothing in the collision numbers to invalidate the given picture of the reaction.

The correlation between the kinetic and thermodynamic interpretations of a chemical equilibrium leads to a relation between the ratio of the collision numbers of the forward and reverse reaction and the standard entropy change. For reactions (3) and (4) this relation is
$R \ln \left(A_{4} / A_{8}\right)=S^{0}\left(\mathrm{Br}^{-}\right)+S^{0}(\mathrm{Cl} A)-\mathrm{S}^{0}\left(\mathrm{Cl}^{-}\right)-S^{0}(\mathrm{Br} A)$
where $S^{0}$ is the molal entropy of the given substance when its concentration is $1 M$ in an ideal aqueous solution, based on $S^{0}\left(\mathrm{H}^{+}\right)=0$ for comparison. Latimer, Schutz and Hicks ${ }^{11}$ give 5.9 e. u. as the difference between $S^{0}\left(\mathrm{Br}^{-}\right)$and $S^{0}$ $\left(\mathrm{Cl}^{-}\right)$. Using this value, and the experimental values of $A_{4}$ and $A_{3}$ we calculate that the difference in entropy between solutions of $l-\mathrm{Br} A$ and $l$ $\mathrm{Cl} A$ is $2.7 \pm 1 \mathrm{e} . \mathrm{u} .$, a not unreasonable result.

Rice and Gershinowitz ${ }^{12}$ have made use of the relation between entropy and collision number to develop a method for calculating the collision numbers of bimolecular associations. The reactions studied can be looked upon as being of this type followed by the almost instantaneous decomposition of the associated pentavalent carbon "complex." We have applied this method in calculating the collision numbers of the four reactions, omitting consideration of vibrational
(10) O. K. Rice, This Journal, 54,4558 (1932)
(11) W. M. Latimer, P. W. Schutz and J. F. G. Hicks, J. Chem. Phys., 2, 82 (1934).
(12) O. K. Rice and H. Gershinowitz, ibid., A, 853 (1934).
entropy, and calculating moments of inertia from rough geometrical models of the reactants. The results are shown in Table XI.

Table XI

|  | Reaction <br> (1) | $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHBrCOOH}+\mathrm{Br}^{-}$ |
| :---: | :---: | :---: |
| (2) | $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHClCOOH}+\mathrm{Cl}^{-}$ | 3.22 |
| calcd. |  |  | | $A \times 10^{-8}$ |
| :---: |
| obsd. |

Considering the nature of the calculation the agreement is striking. All of the features of the general reaction picture (inversion, face centered addition) have been included in the calculation and no additional ones.

## Summary

The specific rates in aqueous solution of the following four reactions, at several temperatures in the interval $15-50^{\circ}$, have been determined.
(1) $l-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CHBrCOOH}+\mathrm{Br}^{-}=$

(2)


It was shown that reaction 4 , which alone provides information on this point, is accompanied by complete inversion in configuration, in accord with the theory.
Thie activation energies of the four reactions bear relations to each other similar to those in the corresponding reactions of the halogenosuccinic acids.

The collision numbers of the four reactions, considered from a kinetic viewpoint, are not in disagreement with what might have been predicted from the theory. They are in close agreement with values calculated by a statistical mechanical method embodying the essential features of the theory.
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